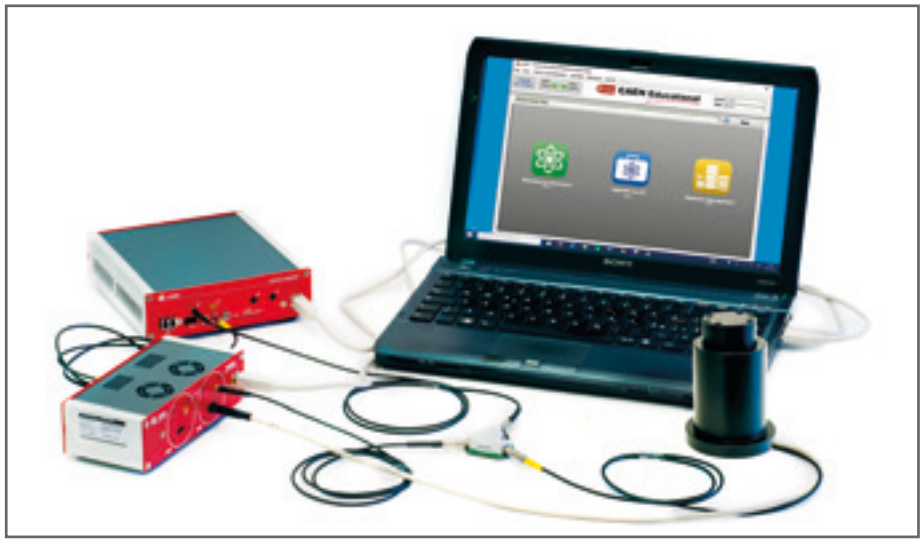
B.1.2 Poisson and Gaussian Distribution

SG6112A



Difficulty	Execution Time	Data Analysis	Radioactive Sources
		YES	YES

Dedicated kit	
Description	pp.
SP5600C Educational Gamma Kit	179

Requirements

Gamma Radioactive Source

Equipment

SP5600C - Educational Gamma Kit

Model	SP5600	DT5720A	A315	SP5606	SP5607
Description	Power Supply and Amplification Unit	Desktop Digitizer 250 MS/s	Splitter	Mini-Spectrometer	Absorption tool
					
	p. 190	p. 190	p. 192	p. 192	p. 193

Purpose of the experiment

Study the statistical distribution of the counting rates of a gamma radioactive source. Comparison of the data to the Poisson distribution, turning into a Gaussian as the mean number of counts grows. The study can be performed both experimentally, with the SiPM kit or simulating it with the emulation kit.

See the Application

Fundamentals

The number of radioactive particles detected over a time Δt is expected to follow a Poisson distribution with mean value μ. It means that for a given radioactive source, the probability that n decays will occur over a given time period Δt is given by:

$$P_\mu(n) = \frac{\mu^n}{n!} e^{-\mu}$$

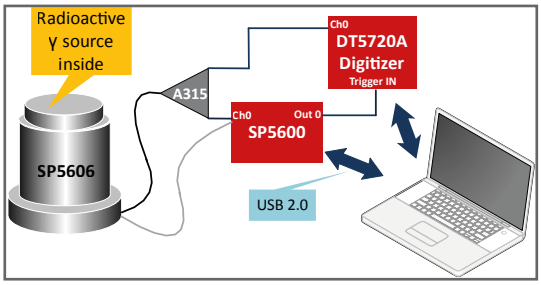
Where μ is proportional to the sample size and to the time Δt and inversely proportional to the half-life $T_{1/2}$ of the unstable nucleus. As long as μ grows, the probability P_μ (n) is well approximated by a Gaussian distribution:

$$P(n) = \frac{1}{\sqrt{2\pi\sigma}} e^{\frac{-(n-\mu)^2}{2\sigma^2}}$$

Where σ = √μ is the standard deviation.

Carrying out the experiment

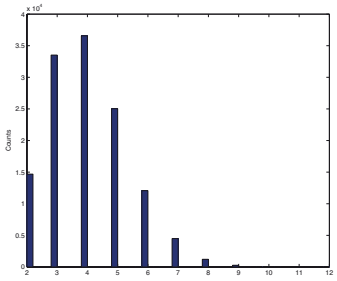
The selected scintillator crystal shall be coupled to the SiPM in the SP5607, through a thin layer of index matching grease to maximize the light collection. In order to avoid saturation, the output of the SiPM is divided using the A315 splitter: one branch is connected to the DT5720A and will be digitized. The other branch will be amplified by the SP5600 module, generating the trigger for the integration signal by the on-board leading edge discriminator or simply counting the pulses induced by the detected gamma ray. The discriminator threshold shall be defined looking at the spectrum and evaluating the dark count rate. Once this is properly set, the counting experiment shall be performed.



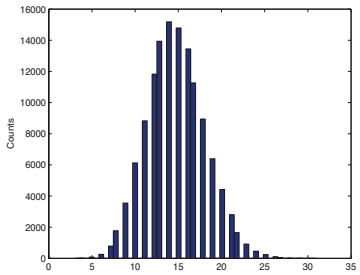
Block diagram of the experimental setup that makes use of the "Educational Gamma Kit" .

Results

Changing the counting window and/or the activity of the source or the threshold, the number of counts changes, with a probability density function moving form a Poissonian to a Gaussian shape. The student may play with the data, fitting them and comparing the expectations to the measurement.



Poissonian distribution.



Gaussian distribution.

This experiment is also possible with the following kits

B SP5600AN
Educational kits
PREMIUM

see p. 179

C SP5640
GammaEDU

see p. 183

D SP5630EN
Environmental kit

see p. 181

E SP5630ENP
Environmental kit Plus

see p. 181

F SP5600EMU
Emulation kit

see p. 180